

# Weak Solvability Theorem for Forward-Backward SDEs.

François Delarue<sup>(a),\*</sup> and Giuseppina Guatteri<sup>(b),†</sup>

(a) Laboratoire de Probabilités et Modèles Aléatoires,  
Université Paris VII, UFR de Mathématiques, Case 7012,  
2, Place Jussieu, 75251 Paris Cedex 05 - FRANCE.

(b) Dipartimento di Matematica, “Francesco Brioschi”, Politecnico di Milano,  
Piazza Leonardo da Vinci, 32, 20 133 Milano - ITALY.

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## Abstract

We aim to establish the existence and uniqueness of weak solutions to a suitable class of non-degenerate deterministic FBSDEs with a one-dimensional backward component. The classical Lipschitz framework is partially weakened: the diffusion matrix and the final condition are assumed to be space Hölder continuous whereas the drift and the backward driver may be discontinuous in  $x$ . The growth of the backward driver is allowed to be at most quadratic with respect to the gradient term.

The strategy holds in three different steps. We first build a well controlled solution to the associated PDE and as a bypass product a weak solution to the forward-backward system. We then adapt the “decoupling strategy” introduced in the *four step scheme* of Ma, Protter and Yong to prove uniqueness.

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\*delarue@math.jussieu.fr (corresponding author)

†guatteri@mate.polimi.it