

# ON THE DAMPED SEMILINEAR WAVE EQUATION WITH CRITICAL EXPONENT

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**Abstract.** We provide an optimal regularity result for the universal attractor of the weakly damped semilinear wave equation, when the nonlinearity satisfies the critical growth condition. This allows us to prove an upper semicontinuity result as well as the existence of an exponential attractor.

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1991 *Mathematics Subject Classification.* Primary: 35B41, 35L05; Secondary: 35L25, 35Q40.

*Key words and phrases.* Damped wave equation, universal attractors, upper semicontinuity, exponential attractors.