Multiple positive solutions for some Schrödinger Equations

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Abstract: We consider the problem

$$(P) \quad \left\{ \begin{array}{ll} -\Delta u + a(x)u = |u|^{p-1}u & \mbox{ in } I\!\!R^N \\ u \in H^1(I\!\!R^N) \end{array} \right.$$

where $N \ge 2$, $p \in (1, \frac{N+2}{N-2})$ and the potential a(x) is a continuous positive function such that

i) $a(x) \to a_{\infty} > 0$ as $|x| \to \infty$,

ii) $a(x) \ge a_{\infty}, \quad a(x) \ne a_{\infty}$

Under suitable assumptions on the decay and on the oscillation of a(x), but without any symmetry assumption, we prove the existence of infinitely many positive solutions of (P).