

Alberto Perelli: *Non-linear twists of L-functions*

Abstract: A non-linear twist of an L -function $L(s)$ is a Dirichlet series of type

$$L(s, \alpha) = \sum_{n=1}^{\infty} a(n) e(-\alpha n^{\kappa}) n^{-s},$$

where $a(n)$ are the Dirichlet coefficients of $L(s)$, $\alpha > 0$ is a variable, $\kappa > 0$ is a given parameter and $e(x) = e^{2\pi i x}$. We also consider multidimensional non-linear twists, where αn^{κ} in the above expression is replaced by $\alpha_1 n^{\kappa_1} + \dots + \alpha_N n^{\kappa_N}$. We present a survey of several results, obtained with J. Kaczorowski, concerning the analytic properties of the non-linear twists and their applications to the problem of the classification of L -functions.