Critical points for vector-valued functions

R.E. Lucchetti, J.P. Revalski and M. Théra

Abstract

This paper contains a mountain pass theorem for continuous mappings, defined on a complete metric space and taking values in a real Banach space, ordered by a closed convex cone. We use the concept of critical point introduced by Degiovanni, Lucchetti and Ribarska, and we furnish a variant of their result, allowing for a localization both of the critical point and of the critical value.

Key words: weak slope, critical point, Palais-Smale condition, mountain pass theorem, Pareto optimum.