

**NONCOMMUTATIVE POTENTIAL THEORY AND THE SIGN
OF THE CURVATURE OPERATOR IN RIEMANNIAN
GEOMETRY.**

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ABSTRACT. The aim of this work is to show that in any complete Riemannian manifold M , without boundary, the curvature operator is nonnegative if and only if the Dirac Laplacian D^2 generates a C^* -Markovian semigroup (i.e. a strongly continuous, completely positive, contraction semigroup) on the Clifford C^* -algebra of M or, equivalently, if and only if the quadratic form \mathcal{E}_D of D^2 is a C^* -Dirichlet form.

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