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behavior of different atheromatous carotid plaques**

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1 FLUID STRUCTURE INTERACTION ANALYSIS TO STRATIFY THE BEHAVIOR OF 2 DIFFERENT ATHEROMATOUS CAROTID PLAQUES

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32 **Key words:** Carotid Stenosis; Carotid Plaque; Carotid Endarterectomy; Computational Fluid Dynamics;
33 Fluid Structure Interaction; Risk Stratification.

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41 **ABSTRACT** (294 words)

42 **Objectives:** Different plaque types could have different hemodynamic and structural behaviors in
43 asymptomatic carotid stenosis (ACS), increasing the risk of instability.

44 **Methods:** The vessel lumen, the wall, and the geometries of three different types of carotid
45 plaques, namely lipid (LP), fibrous (FP), and calcific (CP) were reconstructed starting with CTA
46 images from 15 candidate patients for carotid revascularization with ACS >70%, in order to obtain
47 5 models for each type. Fluid structure interaction (FSI) analyses were performed to describe
48 hemodynamic and structural behavior in different types of plaques by computing wall shear stresses
49 (WSS), plaque displacements (D), von Mises stresses (VMS), and absorbed elastic energy (AEE)
50 spatial distribution and their maximum-in-space values at the systolic peak, namely WSS_{syst} , D_{syst} ,
51 VMS_{syst} and AEE_{syst} .

52 **Results:** WSS_{syst} resulted significantly lower in LP, whereas in FP we found intermediate values
53 (+33%) and the highest WSS_{syst} (+157%) in CP. The highest values of D_{syst} were observed in LP,
54 with a different spatial distribution, being localized mainly in the inner region of the thin fibrous
55 cap, at the shoulder of the stenosis, whereas for FP and CP the values were -250% and -480% lower,
56 respectively. VMS_{syst} in the LP group was again localized to the inner region of the thin fibrous cap,
57 whereas FP and CP had lower values, -150% and -400%, respectively, without spatial concentration
58 of peak stresses. AEE_{syst} was determined to be focused at the fibrous cap, and capable of storing
59 elevated values of energy due to the compliant nature of the inner core in LP, while lower values
60 were found for FP and CP, -470% and -2240%, respectively.

61 **Conclusions:** Depending upon their nature, plaques store different amounts of mechanical energy.
62 The deformation causes different distributions of internal forces inside the plaque, thus influencing
63 vulnerability properties, especially for LP.

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67 **Key words 3-6** CAROTID STENOSIS, CAROTID PLAQUE, CAROTID ENDARTERECTOMY,
68 COMPUTATIONAL FLUID DYNAMICS, FLUID STRUCTURE INTERACTION, RISK
69 STRATIFICATION

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71 Word count: 3938

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74 **What this paper adds:**

75 The measurement of mechanical descriptors such as von Mises stress and, for the first time to the
76 best of our knowledge, the absorbed energy can give better insights on different vulnerability
77 conditions of carotid plaques, thus contributing to a better understanding of the behavior of
78 asymptomatic carotid plaques in relation to their physical nature.

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82 INTRODUCTION

83

84 Cerebral ischemic stroke is one of the leading causes of debilitating neurological disease and death.
85 Large-vessel cervical or intracranial atherosclerosis is the cause of 16% of all ischemic strokes
86 attributed to carotid artery stenosis.¹

87 The surgical treatment of asymptomatic carotid stenosis (ACS) remains controversial. Currently, the
88 major guidelines still advise carotid revascularization in asymptomatic patients when >60% stenosis
89 is detected, but experts' opinions are different and varied. Some authors are questioning if carotid
90 endarterectomy (CEA) is an effective strategy for stroke prevention in ACS, supporting best
91 medical treatment (BMT) as therapy alone,² while others defend the thesis of plaque progression
92 toward symptomatology in a significant percentage of cases notwithstanding contemporary BMT.³
93 There are also middle ground positions which advocate more balanced indications stressing that, per
94 1000 CEAs performed in ACS, only 50 strokes are prevented at 5-years.⁴

95 The identification of high-risk plaque conditions, which considers the degree of carotid stenosis in
96 addition to the composition of the plaque,⁵ could have strong prognostic implications. The concept
97 of plaque vulnerability has evolved over the years, informed by both clinical experience and
98 radiological studies.^{6, 7} Irregular, heterogeneous and soft plaques are more frequently correlated
99 with symptoms and, rapid plaque volume progression in severe narrowing.⁸

100 Computational fluid dynamics (CFD) has been used for the study of carotid blood dynamics to
101 provide indications to guide clinicians.⁹⁻¹² To obtain a characterization of blood dynamics and
102 internal structural forces in plaque, several works considered a fluid structure interaction (FSI)
103 approach.^{13,14} This described the interaction of blood with the plaque and allowed investigation of
104 different plaque typologies.¹⁵

105 The aim of our research was to assess, in ACS patients, the hemodynamic and mechanical behaviors
106 due to different plaque morphologies using FSI analysis empowered by the use of an innovative
107 geometric tool to reconstruct the plaque.¹⁵

108 To investigate the plaque behavior, we computed hemodynamic and mechanical quantities related to
109 plaque vulnerability,¹⁶⁻¹⁷ and proposed an innovative indicator based on the plaque energy to stratify
110 the different plaque typologies.

111

112 **MATERIALS AND METHODS**

113

114 **Selection of patients and imaging reconstruction**

115 Fifteen ACS patients with severe carotid stenosis and candidates for CEA, were selected and
116 submitted to carotid doppler ultrasound (DUS). Preoperative evaluation of the degree of stenosis
117 and plaque typology were performed by a well-trained ultrasonographer (RC). The percentage of
118 stenosis was classified according to the guidelines of the European Society for Vascular Surgery
119 (ESVS).¹⁸

120 Lipid plaques (LP), fibrotic plaques (FP) and calcific plaques (CP) have been identified as
121 according to Gray-Weale classification based on plaque echo-lucency.¹⁹

122 After DUS, all patients were submitted to computed tomographic angiography (CTA) as a part of
123 the preoperative work-up.

124 Ethical review board approval and informed consent were obtained from all patients recruited in the
125 study (FLUIDODINAMIC-AUX 34C002_2020).

126

127 **Geometric reconstruction of lumen, vessel wall and plaque**

128 The surface of the lumen was reconstructed from CTA images with the library VMTK
129 (<http://www.vmtk.org/>) and then turned into computational fluid meshes. To create the mesh of
130 vessel wall and plaque, we used our previously published geometric tool.¹⁵ We geometrically
131 modeled LP as a plaque of type I, with an external layer composed by a thin fibrous cap with a
132 thickness of about 100 μm ;²⁰ FP was modeled as a plaque of type III, formed only by fibrotic

133 material,²¹ whereas CP as a plaque of type V, with compact and coherent calcifications²² covered by
134 a thin fibrous cap (Fig. 1).

135

136 **Fluid-structure interactions analysis**

137 To study the behavior of different plaques, we used a FSI model,²³ where blood was considered as a
138 Newtonian, homogeneous, and incompressible fluid,²⁴ whereas healthy vessel and plaque
139 components as a linear elastic material. A flow waveform with an average flow rate of 248.5
140 mL/min, taken from the literature,²⁵ was assigned at the inlet of the carotid. At each of the outlets, a
141 three element windkessel model²⁶ was considered to simulate the distal vasculature, calibrated as
142 proposed in Groen et al.,²⁷ to obtain suitable flow divisions for different degrees of stenosis (Table
143 1).

144 For the structure problem, we imposed null displacements at the inlet and outlet rings, whereas on
145 the external surface, we applied a set of elastic springs to mimic the surrounding tissue.²⁸ FSI
146 simulations were performed with the Finite Elements library LifeV ([https://bitbucket.org/lifev-](https://bitbucket.org/lifev-dev/lifev-release/wiki/Home)
147 [dev/lifev-release/wiki/Home](https://bitbucket.org/lifev-dev/lifev-release/wiki/Home)).¹⁵ The time step was $1 \cdot 10^{-3}$ s, the Young modulus E was 300 KPa for
148 the healthy vessel,²⁸ 30 KPa for the lipidic core,²⁹ 300 KPa for the fibrous cap,²⁹ and 30 MPa for the
149 calcifications.³⁰

150

151 **Quantities of interest**

152 To describe the role of hemodynamics in determining the vulnerability conditions of the plaque,
153 some specific quantities were computed.

154 *Wall Shear Stresses (WSS)* represents the magnitude of blood tangential forces on the endothelium,
155 causing a stress within the plaque. High values of WSS could induce plaque rupture.³¹ WSS_{sys} is
156 the systolic maximum-in-space WSS.

157 *Displacements (D)* of the plaques which provide information about the plaque stability since high
158 displacements are recognized to be a source of instabilities.³² D_{syst} is the systolic maximum-in-
159 space value of D ;

160 *von Mises Stresses (VMS)*, i.e. structural internal stresses. Areas of the fibrous cap with high values
161 of VMS were correlated with a larger rupture risk.³³ VMS_{syst} is the systolic maximum-in-space
162 VMS;

163 *Absorbed Elastic Energy (AEE)* is the mechanical potential energy, per unit of volume, stored in the
164 plaque during elastic deformation. The systolic maximum-in-space AEE is

$$AEE_{syst} = \frac{(VM_{syst})^2}{2 \cdot E} \text{ [J/m}^3\text{]}.$$

167 **RESULTS**

169 A total of 15 carotids were selected from patients submitted to CEA for >70% ACS. Three
170 typologies of plaque (LP, FP and CP) were analyzed (Table 1), see Fig. 2 for the vessel and plaque
171 computational meshes.

172 We start analyzing the WSS magnitude at the systolic peak (Fig. 3), which resulted significantly
173 high in CP. Accordingly, in FP we found intermediate WSS values, whereas in LP the lowest ones.

174 We computed also the spatial distribution of the displacement magnitude within the plaque (Fig. 4).

175 The highest values were observed for LP group, while the lowest ones for CP. We observed that
176 within the LP group, the maximum values were localized mainly in the inner region of the fibrous
177 cap, at the shoulder of the stenosis, whereas for FP and CP a homogeneous distribution of the
178 displacements around the plaque was observed, with an absence of hotspots.

179 We then analyzed the spatial distribution of VMS at the systolic peak (Fig. 5). In the LP group the
180 areas with higher VMS were located in the inner region of the fibrous cap, whereas in FP and CP
181 lower values without any concentration of peak stresses were found.

182 To better quantify the different mechanical behaviors of plaques subjected to blood forces, we
183 reported the distribution of the 100 highest systolic values of WSS, D and VMS clustered in
184 different intervals (Fig. 6). These results confirmed the lowest WSS values for LP and lowest VMS
185 and D values for CP, together with intermediate values for FP for all the quantities.

186 Considerable attention was paid to determine the spatial distribution of the elastic energy stored by
187 the plaque (Fig. 7). We observed that, in correspondence with the region of the fibrous cap in
188 contact with blood, LP was able to store elevated values of energy. Moreover, the lipidic core
189 absorbed more energy with respect to the calcifications, due to its compliant nature. Table 2
190 summarizes the values of WSS_{syst} , D_{syst} , VMS_{syst} and AEE_{syst} together with the average values for
191 each type of plaque.

192 Regarding WSS_{syst} , the average values for LP were 33% and 157% lower than the corresponding
193 values for FP and CP, respectively. An inverse correlation was found for the mechanical quantities:
194 the average value of D_{syst} for LP was 250% and 480% greater than for FP and CP, respectively,
195 whereas VMS_{syst} was 150% and 400% greater, respectively.

196 Lastly, we determined the average values of AEE_{syst} stored by the plaques. We noticed that the
197 fibrous cap of LP absorbed more (470% to 2240%) energy than FP and CP, respectively, while the
198 lipidic core featured very large values, in average greater by several tens of thousands than in the
199 case of calcifications.

200

201 **DISCUSSION**

202

203 Engineering studies of carotid bifurcation have been recognized as valuable methods for studying
204 the development of atherosclerosis,²⁶ surgical techniques,¹² and restenosis development.³⁴ To further

improve carotid risk stratification, FSI analyses were used to investigate inter-individual variations in blood dynamics and wall mechanics of carotids. Vulnerable sites included all locations where cycling stress and deformation of the plaque can cause focused tissue damage over an area with an underlying lipid core. Gao et al. investigated the impact of fibrous cap thickness and lipid core volume on VMS.²⁹ Tao et al. analyzed VMS, pressure and flow velocity values at the sites of maximum carotid stenosis and found that maximum VMS was significantly higher in the vulnerable plaque cohort than in stable plaques.³⁵

It is also debated whether calcifications act as stabilizers or as exacerbating factors of focal mechanical stress. Li et al., observed that maximum VMS increased by almost 50% when calcium deposits were located in the fibrous cap.³⁶ Wong et al., observed that calcifications structurally stabilize the plaque.³⁷ Mahmoud et al., observed that changes of calcification distribution and size modified stress localization.³⁸

Our study confirmed that FSI analysis is a suitable method to analyze the hemodynamic and structural behaviors of carotid plaques. We have compared different plaque typologies by investigating hemodynamic and structural quantities. We proposed a new way to identify the plaque and differentiate its components utilizing imaging data that are commonly acquired for diagnostic purposes in clinical practice. A particular attention was paid to the analysis of structural quantities, such as D, VMS, and AEE, which was proposed here for the first time to be a potential indicator to highlight the behavior of different plaque typologies subjected to blood flow.

Our study revealed that LP manifests the highest values of D, VMS and AEE within the plaque. Accordingly, the stenotic lumen highly deformed, leading to WSS values significantly lower than the other plaques. On the contrary, CP showed the lowest VMS and D, making this type of plaque similar to a rigid wall and the most stable. FP presented an intermediate behavior with displacements lower than those in LP but higher than CP ones.

Our computational results highlighted also a positive correlation between the plaque Young's modulus E and blood forces. Indeed, large values of E lead to small lumen expansion and therefore,

231 according to Bernoulli's principle, to higher values of WSS, which provoked internal forces within
232 the plaque that could increase its vulnerability. However, looking at Figs. 5 and 6 and Table 2, VMS
233 was highest in LP, where WSS had the lowest values. By observing Fig. 7, we can see that the
234 lipidic core, deformed by the action of blood flow, stored more elastic energy with respect to
235 calcifications, due to its increased compliance (low Young's modulus). This amount of deformation
236 energy is then transmitted to the fibrous cap, leading to a localized increase of mechanical stresses,
237 ³⁹ especially in the area between the lumen and the lipidic core. This mechanism can explain why
238 LP featured the highest values of VMS. On the contrary, the calcification was able to transmit only
239 a small quantity of deformation energy to the covering fibrous cap, due to its stiff nature (high
240 Young's modulus), thus resulting in lower values for internal forces.⁴⁰ Our analysis showed that FP
241 stored more energy than CP but less than LP, leading to intermediate values of VMS. The fibrous
242 tissue provides more structural integrity to the plaque, compared to the lipidic core.⁴¹
243 In summary, these results suggested that different plaque components could act like a spring. Under
244 the action of the blood, they store different amounts of potential mechanical energy, inversely
245 proportional to their elastic modulus, transferring it to the fibrous cap. This amount of deformation
246 is absorbed by the fibrous cap and causes different distribution of internal forces and thus different
247 vulnerability properties. In particular, the lipidic core exerts a key role in making the thin fibrous
248 cap more vulnerable to rupture, leading to the highest values of VMS. Regarding CP, the presence
249 of calcium deposits stabilized the structure by lowering D, AEE, and the internal forces, making the
250 whole plaque less vulnerable.

251 For all these reasons, our proposal to use the AEE proved to be promising to differentiate the
252 mechanical outcomes of the different plaque typologies in view of assessing their vulnerability.

253 From a clinical point of view, carotid vulnerability is a multifactorial process that involves, among
254 other factors, the hemodynamics.⁴² Indeed, rupture takes place preferentially where the mechanical
255 stress exceeds the ultimate strength of the cap material. In this regard, carotid plaques more prone to
256 be symptomatic usually have lipidic core and thinner fibrous cap.⁴³

257 The management of 60-99% ACS remains a debated matter. The degree of stenosis is the main
258 criterion used to indicate intervention but remains unclear which patients will really benefit from
259 intervention. Kamtchum-Tatuene et al., in a recent meta-analysis on ACS patients, identified that
260 the so defined “high-risk plaque” represented up to 26.5% of cases with an overall incidence of
261 cerebrovascular events higher than currently accepted estimates.⁴⁴
262 Nicolaides et al., first proposed combining clinical findings with ultrasonographic features in an
263 effort to identify the carotid vulnerable plaques.⁴⁵ Naylor et al. tried to determine from the
264 Asymptomatic Carotid Atherosclerosis Study (ACAS) and Asymptomatic Carotid Surgery Trial 1
265 (ACST-1) predictive algorithms and imaging parameters able to detect the true ACS at risk.⁴⁶
266 ESVS Clinical guidelines highlighted that the presence of a large juxta-luminal black area on
267 computerized plaque analysis, plaque echo-lucency, or imaging of intra-plaque hemorrhage on
268 MRI, might be useful for the selection of the most proper candidates for CEA.¹⁸
269 Our findings led us to some considerations regarding ACS management. Are all the 60-99% ACS
270 harmless? Or should we consider all lipid plaques potentially vulnerable and worthy of preventive
271 surgical treatment? What should be the correct timing for surgery, considering plaque
272 characteristic?
273 Although some “old” controversies remain in defining the role of surgery in ACS, any effort to
274 better clarify this issue could help determine how to make this important decision.

275

276 **Limitations**

277 A limitation of this study is related to the absence of any biological evaluation of factors involved in
278 the mechanism of plaque growth and rupture and to the absence of histological or imaging-based
279 analysis of the components of the carotid plaque. However, the aim of the work was precisely to
280 develop a method to be used in absence of such information.

281 Finally, FSI modeling was performed on plaques considered completely homogenous. The analysis
282 of non-homogeneous carotid plaques will be the object of future work which will analyze how these
283 conditions could impact their properties and vulnerabilities.

284

285 **CONCLUSIONS**

286

287 Advances in the comprehension of carotid plaque behavior can develop new methods of assessment
288 for stroke risk prediction based more on the individual setting. FSI studies have denoted that LP
289 experienced huge differences in structural and hemodynamic stresses when compared to FP and CP.
290 Even if the absolute magnitude of these values remains small, however, this stress repeated millions
291 of times could exacerbate the insurgence of plaque disruption and cerebrovascular events. Further
292 prospective studies are needed to validate and quantify these findings, to better stratify plaque
293 vulnerability and to provide robust results useful to identify ACS in more vulnerable subgroups
294 which consequently could benefit from preventive revascularization.

295

296

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303

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Table 1. Dataset of the population under investigation. Q_{ICA} = Flux of Internal Carotid Artery; Q_{CCA} = Flux of the Common Carotid Artery.

Patient	Age	Sex	% of stenosis	Type of plaque	Q_{ICA}/Q_{CCA}
LP1	62	M	75	Lipidic	0.7
LP2	71	M	75	Lipidic	0.7
LP3	81	M	80	Lipidic	0.625
LP4	84	M	85	Lipidic	0.55
LP5	82	M	90	Lipidic	0.475
FP1	74	M	75	Fibrous	0.7
FP2	84	M	85	Fibrous	0.55
FP3	66	M	90	Fibrous	0.475
FP4	84	M	90	Fibrous	0.475
FP5	83	M	90	Fibrous	0.475
CP1	84	M	80	Calcific	0.625
CP2	61	F	80	Calcific	0.625
CP3	61	F	85	Calcific	0.55
CP4	68	F	90	Calcific	0.475
CP5	74	F	90	Calcific	0.475

Table 2. Values of WSS_{syst} at the stenosis, D_{syst} , VMS_{syst} and AEE_{syst} within the fibrous cap and within the plaque component. Average values of all the quantities for each type of plaque are also presented.

Patient	WSS_{syst} [Pa]	Average [Pa]	D_{syst} [mm]	Average [mm]	VMS_{syst} [KPa]	Average [KPa]	AEE_{syst} fibrous cap [J/m ³]	Average [J/m ³]	
LP1	63	79	0.22	0.21	41	37	2800	2320	
LP2	55		0.21		40		2666		
LP3	76		0.23		36		2160		
LP4	62		0.16		36		2160		
LP5	140		0.22		33		1815		
FP1	66	105 (+33%)	0.05	0.06 (-250%)	13	15 (-150%)	282	408 (-470%)	
FP2	118		0.08		18		540		
FP3	116		0.09		14		330		
FP4	117		0.07		14		336		
FP5	110		0.01		18		555		
CP1	98	203 (+157%)	0.030	0.036 (-480%)	6	7.4 (-400%)	60	99 (-2240%)	
CP2	120		0.032		5		42		
CP3	140		0.034		8		110		
CP4	282		0.045		9		140		
CP5	377		0.040		9		140		

FIGURES CAPTIONS

Figure 1. Geometric reconstruction of the vessel lumen and of the three types of carotid plaques.

Red: healthy vessel; Light blue: fibrous cup; Yellow: lipidic core; Grey: calcifications; Orange: lumen.

Figure 2. Structure meshes were generated by means of our geometric tool ²³. Red: healthy vessel;

Light blue: fibrous cup; Yellow: lipidic core; Grey: calcifications; Orange: lumen.

Figure 3. Spatial distribution of wall shear stress (WSS) magnitude at the systolic peak. Top: Lipidic plaques (LP); Middle: Fibrotic plaques (FP); Bottom: Calcific plaques (CP).

Figure 4. Spatial distribution of the magnitude of the plaque structure displacements (D) at systolic peak within the plaque. Top: Lipidic plaques (LP); Middle: Fibrotic plaques (FP); Bottom: Calcific plaques (CP).

Figure 5. Spatial distribution of Von Mises stresses (VMS) at systolic peak within the plaque. Top: Lipidic plaque (LP); Middle: Fibrotic plaques (FP); Bottom: Calcific plaques (CP).

Figure 6. Distribution of the 100 highest values for WSS (a), D (b) and plaque VMS (c) for all the different plaques at the systolic peak. Values are intended as magnitudes of the corresponding field.

Figure 7. Spatial distribution of the Absorbed Elastic Energy (AEE) at the systolic peak, during the deformation of the fibrous cap and of the lipidic core and calcifications. Top: Lipidic plaques; Middle: Fibrous plaques; Down: Calcific plaques. Legend on the left refers to the distribution in the fibrous part reported over sections around the stenotic lumen; legend on the right refers to the lipidic and calcified parts reported over the internal plaque surface.

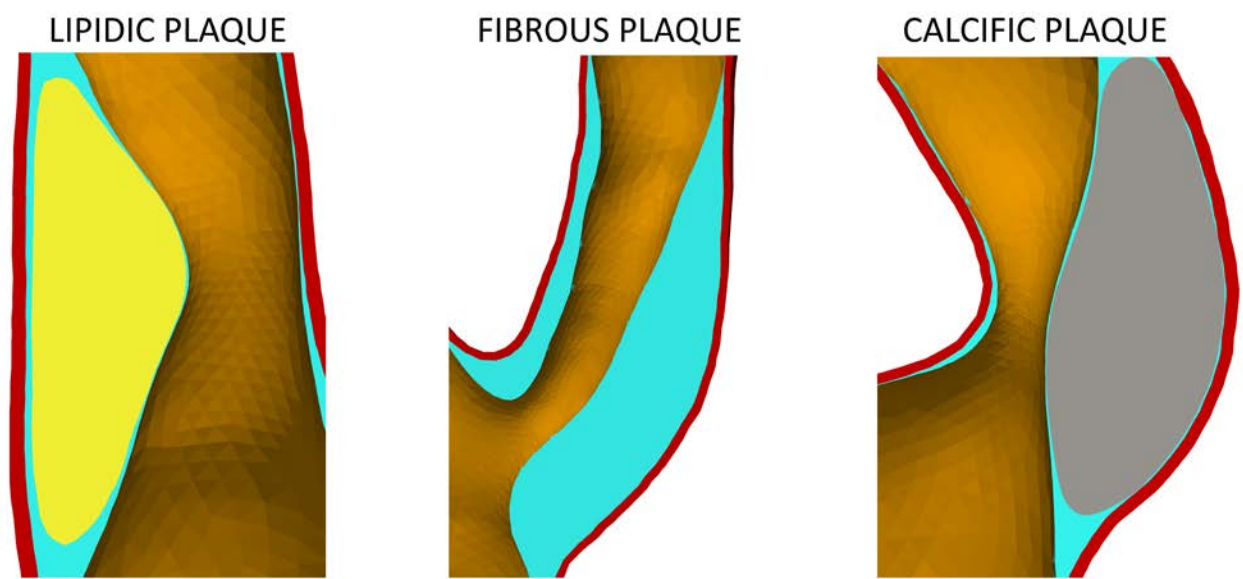


Fig. 1

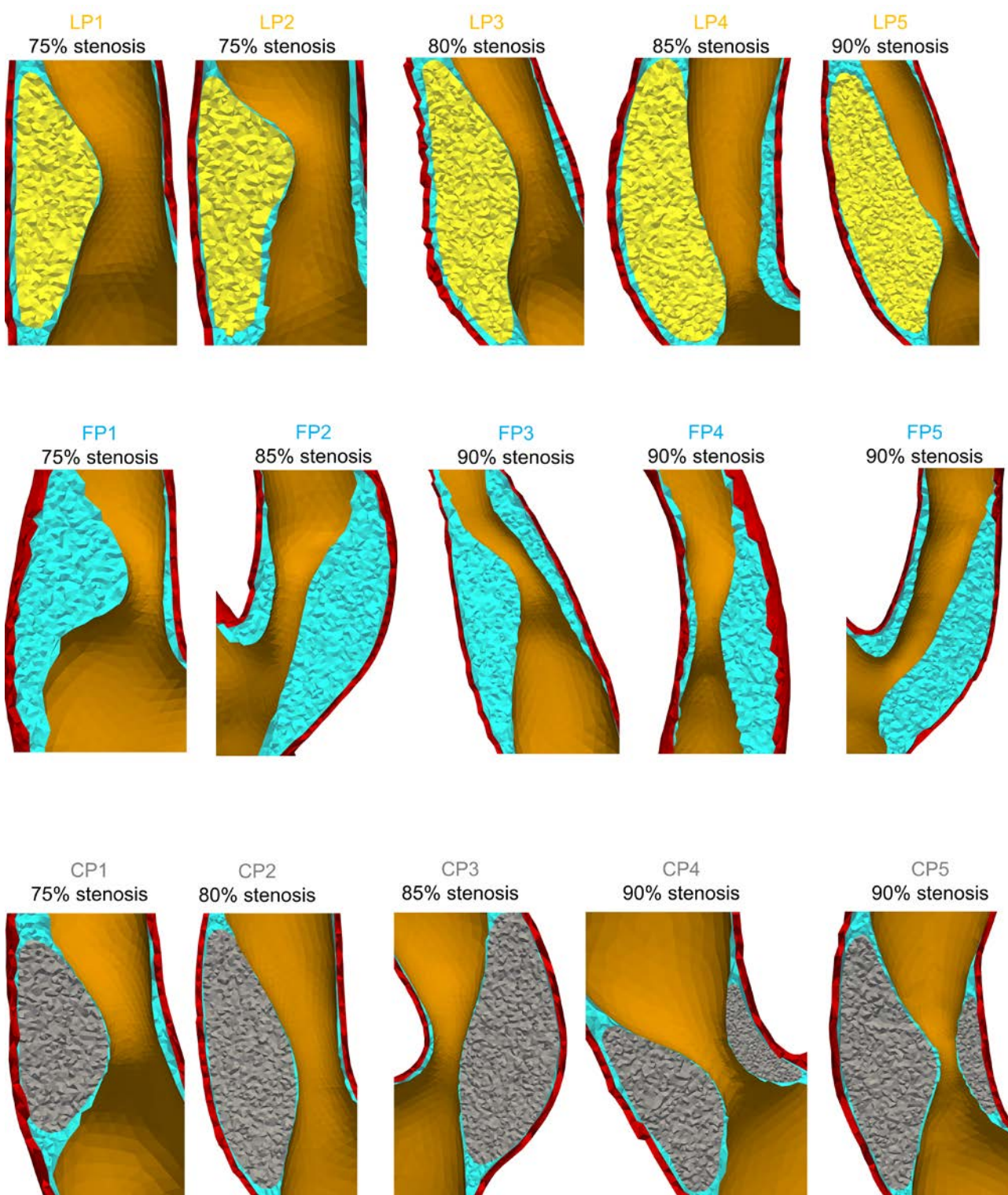


Fig. 2

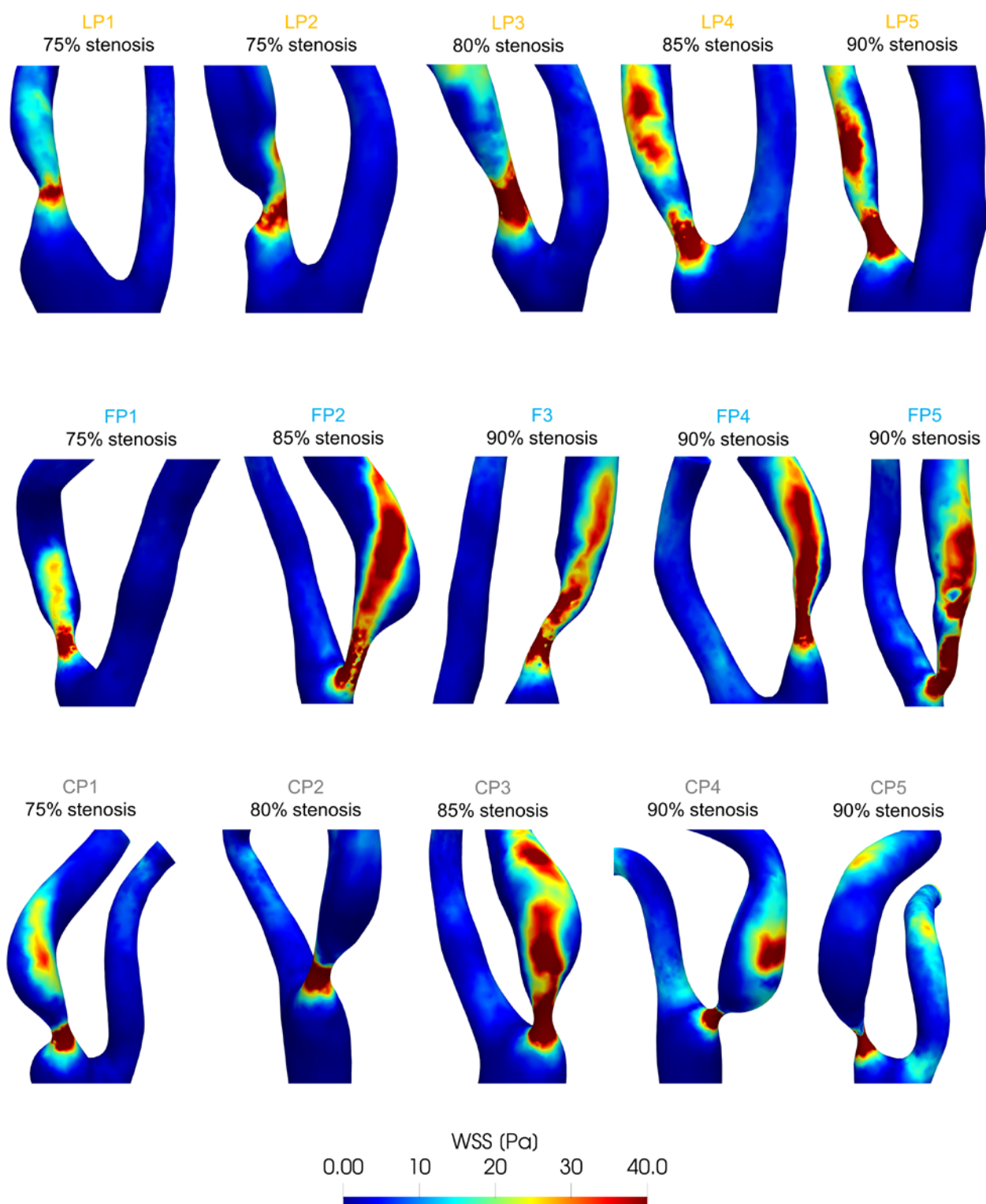


Fig. 3

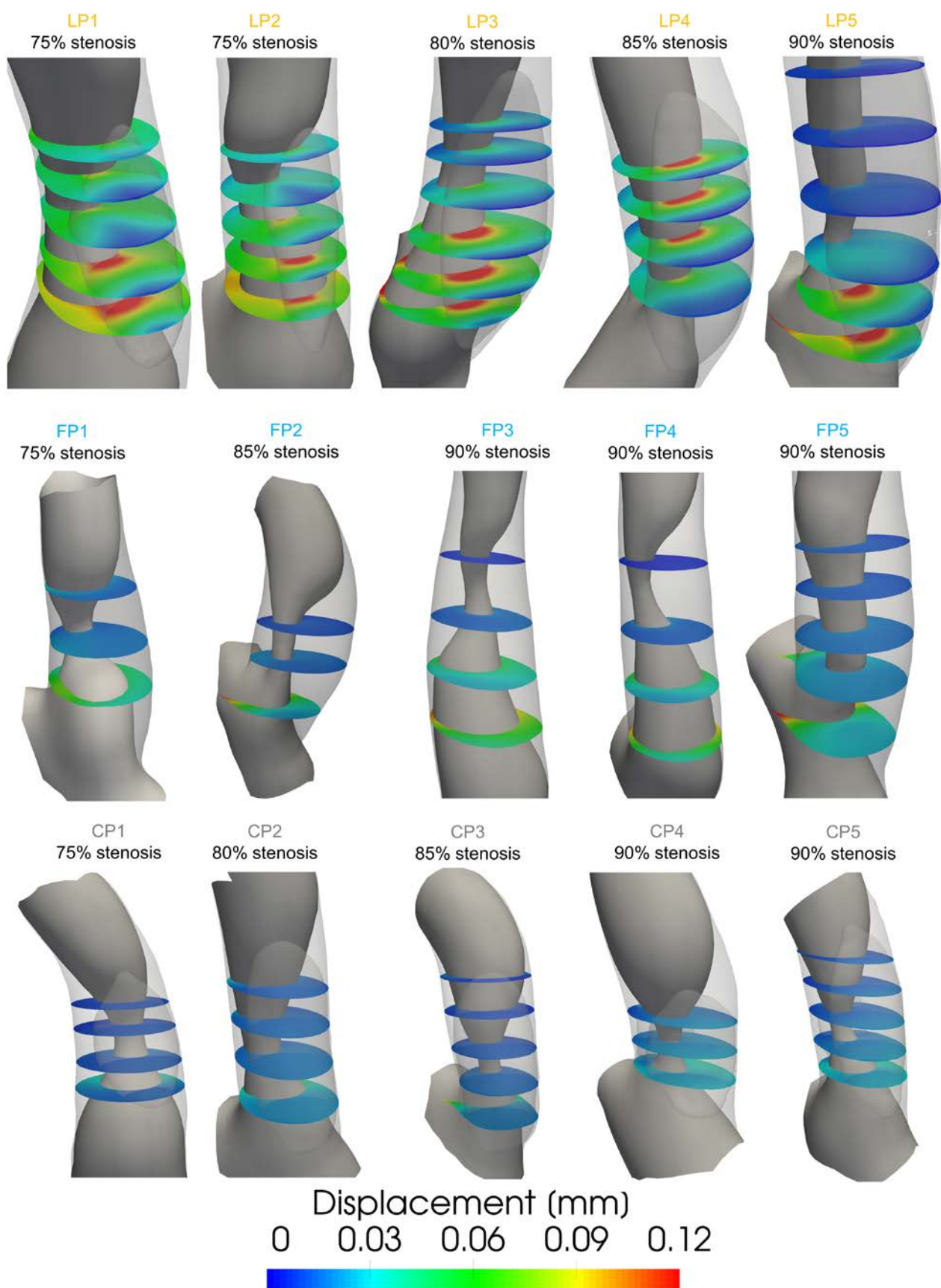


Fig. 4

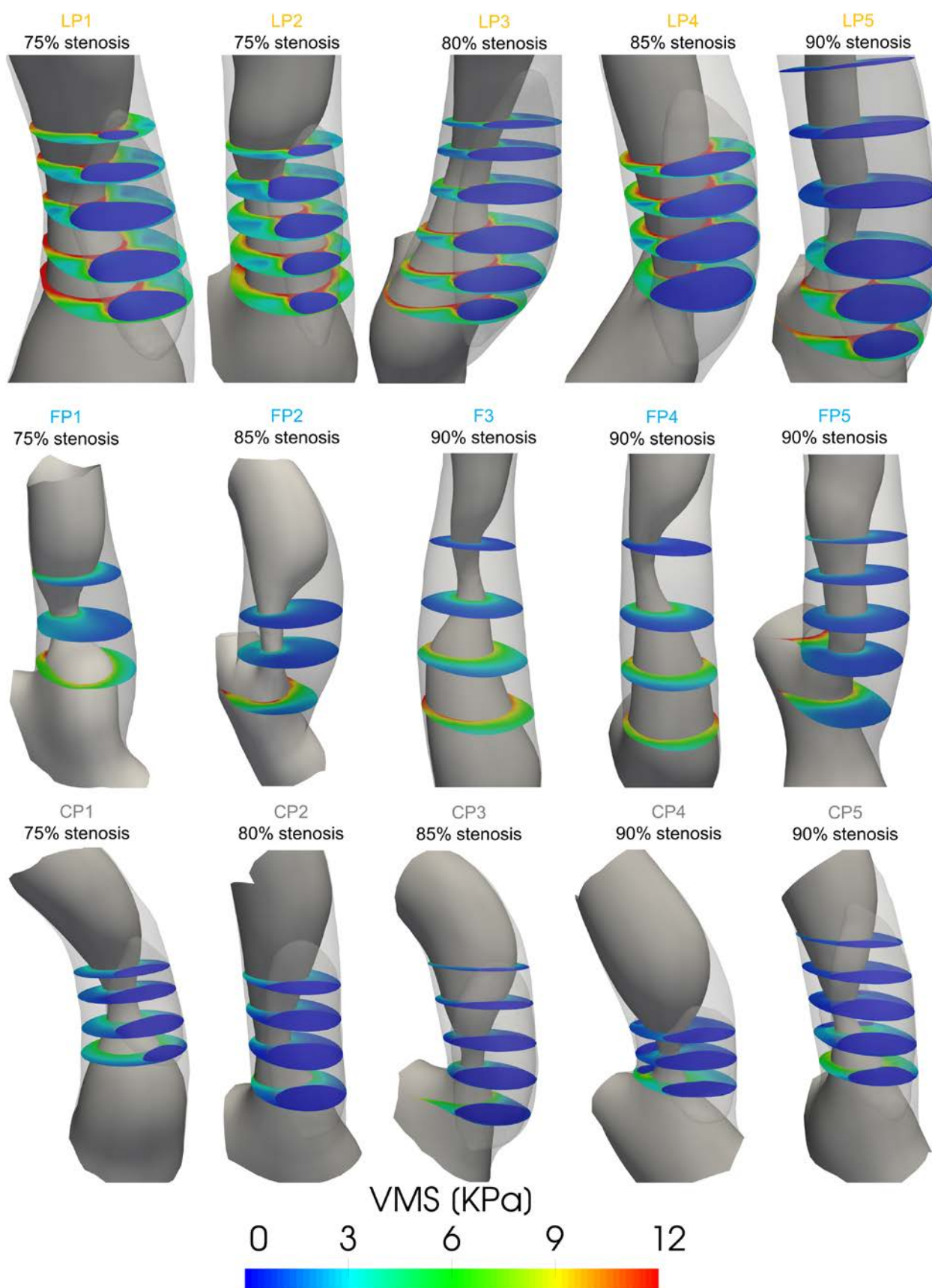


Fig. 5

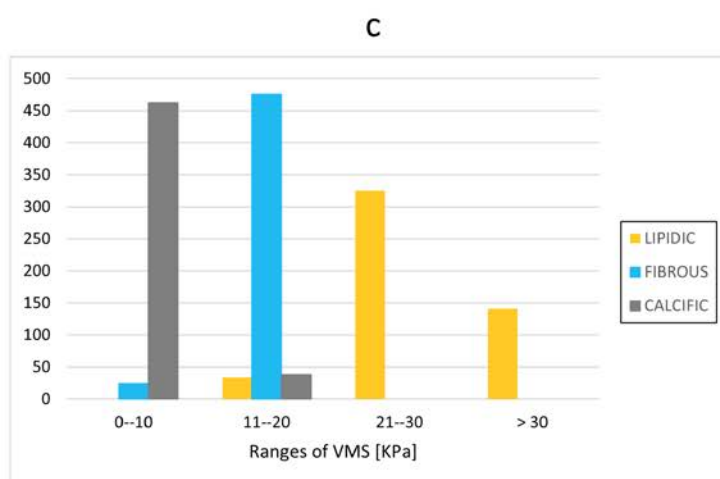
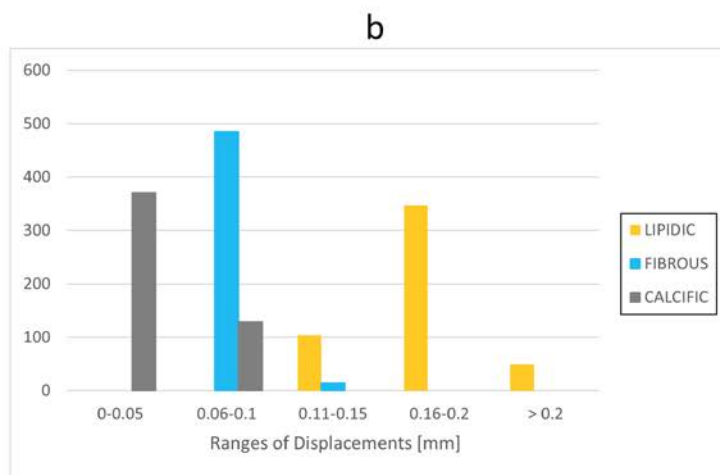
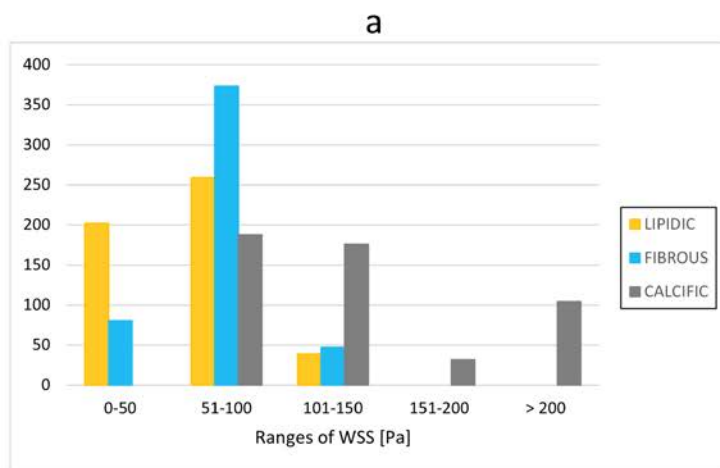


Fig. 6

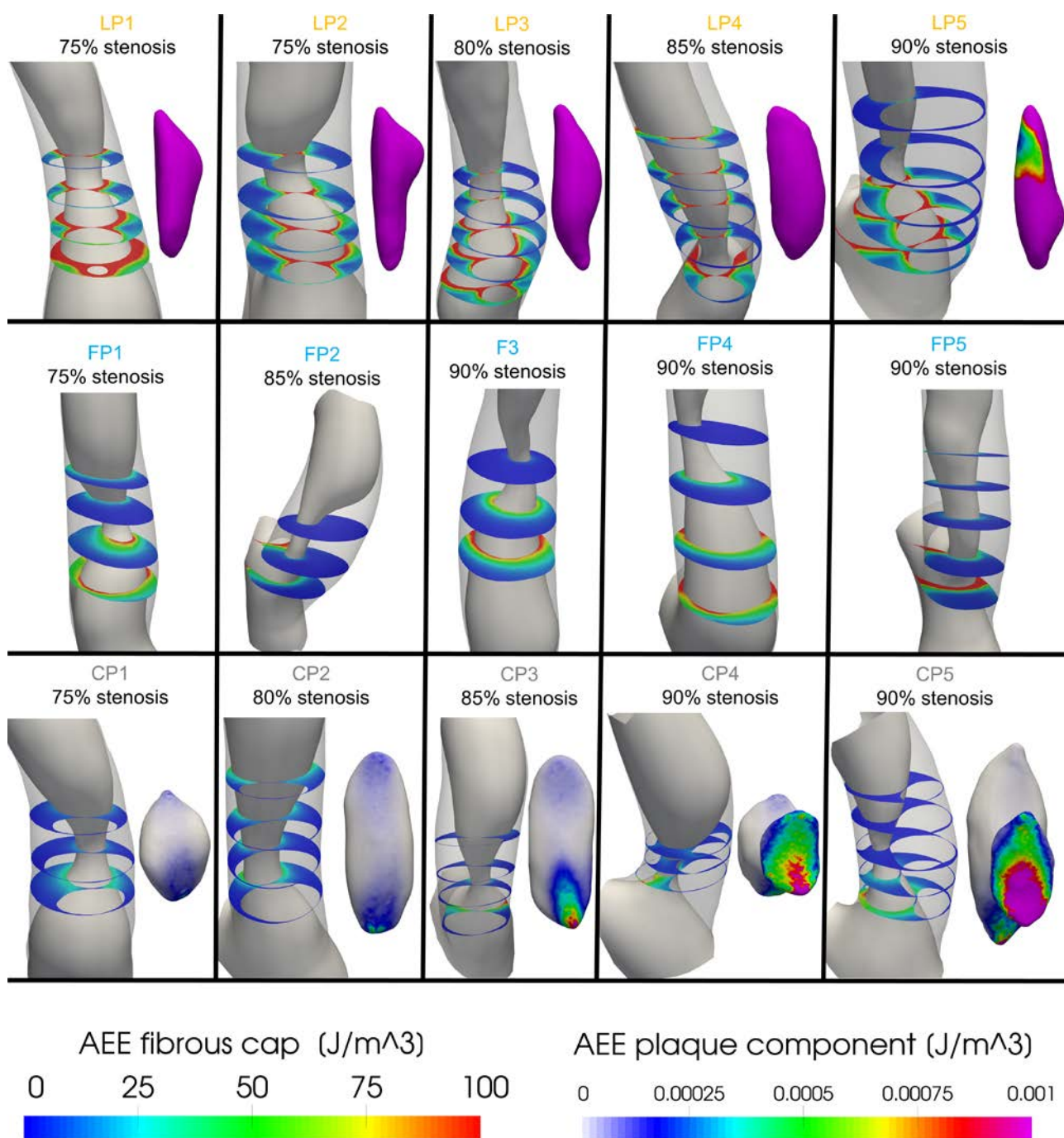


Fig. 7

SUPPLEMENTARY MATERIAL

Computational fluid meshes was composed of about 220k tetrahedra with 3 boundary layers. This corresponds to a representative value of the space discretization of about 0.05 cm far from the stenosis and about 0.01 cm at the stenosis. These values were based on a mesh convergence analysis that showed that further mesh refining would have produced a negligible difference in the computed WSS. The structure (healthy vessel and plaque) meshes were composed of about 300k tetrahedra. The value of the space discretization parameters was set to 0.1 cm for all structure meshes.

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