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Social and material vulnerability in the face of seismic hazard: an analysis of the Italian case

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Abstract

The assessment of the vulnerability of a community endangerd by seismic hazard is of paramount importance for planning a precision policy aimed at the prevention and reduction of its seismic risk. We aim at measuring the vulnerability of the Italian municipalities exposed to seismic hazard, by analyzing the open data offered by the Mappa dei Rischi dei Comuni Italiani provided by ISTAT, the Italian National Institute of Statistics. Encompassing the Index of Social and Material Vulnerability already computed by ISTAT, we also consider as referents of the latent social and material vulnerability of a community, its demographic dynamics and the age of the building stock where the community resides. Fusing the analyses of different indicators, within the context of seismic risk we offer a tentative ranking of the Italian municipalities in terms of their social and material vulnerability, together with differential profiles of their dominant fragilities which constitute the basis for planning precision policies aimed at seismic risk prevention and reduction.

1 Introduction

After the tragic sequence of earthquakes near Amatrice in 2016, the Italian government set up the Casa Italia task force¹ to develop a plan for housing and

¹The task force Casa Italia of the Italian Presidency of the Council of Ministers was established on September 23, 2016. Its members were Giovanni Azzone (Project Manager and Scientific Director), Massimo Alvisi, Michela Arnaboldi, Alessandro Balducci, Marco Cammelli, Guido Corso, Francesco Curci, Daniela De Leo, Carlo Doglioni, Andrea Flori, Manuela Grecchi, Massimo Livi Bacci, Maurizio Milan, Alessandra Menafoglio, Pietro Petraroia, Fabio Pammolli, Davide Rampello, Piercesare Secchi. The 3rd of July 2017, the Italian Presidency of the Coun-

land care directed to the better protection of citizens, and public and private goods, against natural risks. One of the first activities of Casa Italia was aimed at integrating and enhancing the rich information on natural risks already available as the result of numerous and continuing investigations carried out by several national institutions². The action was devoted to identify the sources of information and the data bases allowing for a unified and integrated vision of the natural risks insisting on the Italian territory, with particular reference to the three factors that compose risk, namely, hazard, vulnerability and exposure. Consistent with the mission of Casa Italia, the survey was limited to databases that (a) were elaborated by official and national research institutes, (b) had coverage of the entire national territory, and (c) had a spatial resolution sufficient to allow identification and comparison of local specificities. Believing that it is the community, more than the single individual, which should be the collective principal agent of the prevention endeavor against natural risks, the municipality (*Comune*, in Italian) was identified as the smallest spatial statistical unit for the actual analyses. The product of this action is the Mappa dei Rischi dei Comuni $Italiani^3$ (MRCI), which was presented to the public on February 18, 2019 by the Department Casa Italia – a meanwhile established permanent division of the Italian Government, derived from the positive experience of the Casa Italia task force which terminated its activities in May 2018. The MRCI is a freely accessible web portal implemented by ISTAT, the Italian institute providing official statistics of the country. The portal supplies integrated information on different natural risks of Italian municipalities - such as earthquake, flooding, landslide, volcano eruption - in conjunction with socio-economic and demographic data. With the aim of creating a widespread awareness of the fragility of the Italian territory, the MRCI offers the possibility of viewing and downloading indicators, charts and maps, together with guided interactive features for data searching and filtering.

Amongst the indicators of natural risks available in the MRCI, the focus of this work is on those allowing to quantify the risk from earthquake. As a matter of fact, prevention of seismic risk can only act on the reduction of the vulnerability of the communities endangerd by it, when the option of reducing their exposition by moving them to a less hazardous territory is excluded [28]. To develop precision policies for seismic risk prevention, it is therefore of paramount importance to understand and quantify the distinctive vulnerability of each community facing a seismic hazard, interpreted as its inability to withstand the consequences of a

cil of Ministers estabilished Casa Italia as one of its departments, committed to the prevention against natural risks (http://www.casaitalia.governo.it/it/). The task force Casa Italia finished its mission on May 31, 2018, while the department Casa Italia is still continuing its activities. The authors acknowledge the task force Casa Italia for the scientific discussions that were inspirational to the present work.

²The institutions consulted by the task force Casa Italia were, in alphabetical order: CNR -Consiglio Nazionale delle Ricerche; ENEA - Agenzia nazionale per le nuove tecnologie, l'energia e lo sviluppo economico sostenibile; INGV - Istituto Nazionale di Geofisica e Vulcanologia; IS-PRA - Istituto Superiore per la Protezione e la Ricerca Ambientale; ISTAT- Istituto Nazionale di Statistica; MIBACT -Ministero per i beni e le attività culturali e per il turismo.

³ http://www4.istat.it/it/mappa-rischi

catastrophic seismic event [32].

An emerging body of literature is devoted to the assessment of social vulnerability to natural hazards based on statistical indicators (see, e.g., [7, 34, 9, 10] and references therein), but only a very small part of it is focused on the case of Italy [11, 12, 13], although the country is amongst the most exposed to natural risks [15]. To our knowledge, the recent study presented in [14] is the only available work that investigates social vulnerability to seismic hazard in Italy. To capture social vulnerability, these authors studied a number of socio-economic indicators made available by ISTAT, and related with age, employment, education, anthropization. As highlighted in [11], social vulnerability should not be interpreted as a stand-alone concept, but rather as context-dependent and associated with the extreme event considered – earthquakes in this work. Considering the community standing on a seismic landscape as made of humans interacting with structures and infrastructures, is thus key to provide sensible assessments of its vulnerability to seismic events and drive decision makers to policy planning. In this work we explore the MRCI with the goal of eliciting from this database the multidimensional aspects outlining the vulnerability of Italian municipalities facing seismic hazard. Unlike previous works, to define and measure the vulnerability of a community endangered by seismic hazard, we believe it is of the greatest importance to include a factor capturing the material vulnerability of the dwelling occupied by the community. Hence, beside the consideration of the socio-economic factors related to its poverty, employment and education, and those related to its demographic dynamics, we will also consider the age distribution of the building stock lived in by the community as a key indicator influencing both its social and material vulnerability, being the age of the building stock directly related to the safety and quality of the places where the community lives. To emphasize this expanded concept of vulnerability in the face of seismic hazard, we refer to it as the social and material vulnerability of a community and we consider it to be the determinant on which precision policies can act upon for the reduction of seismic risk.

The remaining of the paper is organized as follows. In Section 2 we set out the Italian seismic landscape through a summary indicator which is apt to describe the seismic hazard faced by Italian municipalities. This is the landscape the social communities live upon, and on this landscape we project our assessments of social and material vulnerability. Section 3 introduces an index of social and material vulnerability, IVSM, which is already produced by ISTAT. We will identify the spatial hot spots of IVSM and segment them according to seismic hazard. Arguing that IVSM is not sufficient to characterize the social and material vulnerability of the Italian municipalities for the purpose of designing precision policies for seismic risk prevention, we will then analyze two other factors which we believe have an impact on a community's fragility when confronted with a seismic event: the demographic growth and age of the residents, and the age of the building stock they live in. These analyses will be carried out in Section 4 and Section 5, respectively. Ultimately, in Section 6, we will aggregate this analyses with the spatial analysis of IVSM to provide a tentative ranking of Italian municipalities in terms of their social and material vulnerability to seismic

hazard. A final section with further supporting arguments and analyses, and a section with conclusions, will close the paper.

Data and code used to elaborate the results reported in this paper are freely available at the following location: https://github.com/alexdidkovskyi/MRCI_paper

2 The seismic hazard landscape

We cannot act on and change seismic hazard. This is a given landscape social communities must live upon; on this landscape we should evaluate their vulnerability.

The seismic hazard at a given point on the Earth surface can be measured in different ways. In engineering application, a commonly used quantity, often plotted in seismic hazard maps, is the Peak Ground Acceleration (PGA), indicated in the literature as a(q) [20]. This represents the maximum horizontal acceleration on rigid soil which is exceeded with a given probability p, say p = 0.1, in 50 years. The unit of measure of a(g) is g, the acceleration due to Earth's gravity. In Italy, the values of a(g) are determined by the National Institute of Geophysics and Vulcanology (INGV), through the analysis of a national catalogue collecting the location and magnitude of the seismic events registered in Italy since AD 1000. INGV provides estimates of a(q) over a grid of step 0.02 degrees covering the entire Italian territory. Based on these estimates, the MRCI supplies two aggregated summaries of a(g) at the municipality scale: AGMAX_50 and $AGMIN_{50}$, quantifying the maximum and minimum value of a(q), respectively, taken on the grid points lying within the boundaries of the municipality territorial area. As suggested in [28], in this paper we shall conservatively consider $AGMAX_{50}$ – in the following, named ag[max] as in [28] – to represent the seismic landscape of the country.

Figure 1 shows the map of Italy where each municipality has been colored according to ag[max]. The figure also shows the map contour lines partitioning the seismic landscape of the country according to four classes of ag[max], as defined in [28] based on the Italian regulation⁴:

- 1. Low hazard: 0 0.05
- 2. Moderate hazard: 0.05 0.15
- 3. Medium hazard: 0.15 0.25
- 4. High hazard: 0.25 +

 $^{^4 \}rm Opcm$ n. 3519 del 28 aprile 2006: criteri generali per l'individuazione delle zone sismiche e per la formazione e l'aggiornamento degli elenchi delle stesse zone



Figure (1) Map of Italy where each municipality has been colored according to ag[max].

3 The baseline index of social and material vulnerability

For each municipality, the MRCI supplies the value of the Social and Material Vulnerability Index (IVSM, for Indice di Vulnerabilità Sociale e Materiale, in Italian), as defined for the Italian census 2011. IVSM is a scalar meta-index, computed by ISTAT on the basis of seven different socio-economic indicators: the incidence of population with age between 25 and 64 that is illiterate or without qualification; the incidence of families with at least 6 members; the incidence of single parent families (with age of parent up to 64) over the total of families; the incidence of families with possible welfare poverty; the incidence of population living in severely crowded conditions; the incidence of young people (15-29) years) without occupation; the incidence of families with children with potential economic poverty. The index is an Adjusted Mazziotta-Pareto Index [18] which allows for comparison of municipalities across space and time; for more details we refer to [17, 16]. The IVSM index is an estimate of the overall socio-economic vulnerability of a municipality. By construction, all values of IVSM range in the interval (70,130). High values of the index indicate high vulnerability, while low values indicate low vulnerability; the reference value of 100 corresponds to the value of IVSM for the entire country in 1991.

We take IVSM to provide a baseline indication of the inability of the social community (identified as the municipality) to withstand the adverse impacts caused by catastrophic seismic events, and to be resilient to its risk. Figure 2



Figure (2) Map of Italy where each municipality has been colored according to its IVSM

shows the value of IVSM for all the Italian municipalities. One can observe the spatial heterogeneity of the index across the country, although a general trend is also apparent. In the North, values of IVSM are typically low, while its highest values are located in the South of the peninsula and in Sicily. Our first analysis aims at the identification of spatial hot spots for IVSM, i.e., areal clusters where the local spatial correlation of the index is significant. For this purpose we use the Local Indicator of Spatial Association (LISA) first introduced in [5]. To make the paper self-consistent, a short recap on the measures of spatial association we are going to use is in order.

Consider a spatial domain D partitioned in n areal spatial units. The goal is to measure the spatial association between the values of a variable of interest observed at nearby spatial units. Let x_i be the value of the variable observed at the spatial unit i. For instance, x_i is the value of IVSM for the i-th municipality. For any pair (i, j) of spatial units, let w_{ij} be a weight representing the degree of proximity between i and j. The Moran's global index [21] of spatial association is defined as

$$I = \frac{n}{\sum_{i,j} w_{i,j}} \frac{\sum_{i} \sum_{j} (x_i - \bar{x}) w_{ij} (x_j - \bar{x})}{\sum_{i} (x_i - \bar{x})^2}$$

where $\bar{x} = (1/n) \sum_{i} x_i$ is the sample mean of the variable x taken over all the n areal spatial units. The analysis of spatial association is commonly based on standardized variables and on row-wise normalized spatial weights, i.e. $\sum_{j=1}^{n} w_{ij} = 1$ for all *i*. In this paper, we will adopt the common practice to set $w_{ij} = 1/n_i$ if there is a common border between the units *i* and *j*, n_i being the number of neighbouring units of the unit i, and $w_{ij} = 0$ otherwise. Let \tilde{x}_i be the weighted average (named *spatial lag*) of the values of the standardized variable x in the neighbour of the spatial unit i. Then the expression of Moran's I statistic is simplified to

$$I = \frac{1}{n} \sum_{i} x_i \tilde{x_i} \tag{1}$$

which is the correlation coefficient between the values of the variable x and their spatial lags.

The Local Indicator of Spatial Association map (LISA map) [5] identifies spatial units significantly contributing to the global Moran's I index. Indeed consider the term

$$I_i = x_i \tilde{x_i} \tag{2}$$

appearing in the sum defining Moran's I index (1), as the measure of the local spatial association for the variable x. On a LISA map the spatial unit i is highlighted if the local association quantified by the statistic I_i is significantly positive or negative, i.e., the null hypothesis of no autocorrelation is rejected at a certain level of significance. The hypothesis is tested via a permutation scheme [5, 6] where observed values of x are randomly reallocated to the areal units, except for the value x_i which is kept fixed. For each random pattern, the statistic I_i is recomputed; the resulting empirical distribution is used as the reference distribution for the statistic under the null hypothesis of no autocorrelation, i.e. to quantify how extreme is the observed value of I_i under the complete spatial randomness (CRS, see, e.g., [8]) assumption. Note that significance of the local autocorrelation depends only on the significance of the spatial lag \tilde{x}_i (with respect to the null distribution of CSR), since the value x_i is kept fixed. Significance of the local autocorrelation leads to four possible occurrences: (i) High-High, (ii) Low-Low, (iii) Low-High, (iv) High-Low. High-High (Low-Low) singles out a hot spot, a spatial unit where the value of x_i is positive (negative) and the spatial lag \tilde{x}_i is significantly high (low) with respect to the null distribution. On the contrary, Low-High (High-Low) indicates an *outlier* spatial unit, where the value of x_i is negative (positive) but the spatial lag \tilde{x}_i is significantly high (low) with respect to the null distribution.

Hereafter, Moran's I global indexes are computed using the R-package ape [23]. To compute LISA maps along the approach provided in the Python library PySAL [30], we built an *ad-hoc* R-code, available in the github account indicated in the Introduction. For the LISA maps presented in this work, the level of significance is always set to be $\alpha = 0.05$.

The Moran's I global statistic measuring the spatial autocorrelation of IVSM is equal to 0.644. Figure 3a shows the LISA map of IVSM for Italy. The High-High red hot spots where IVSM assumes significant high values are spreading inside the country from the coast in Lazio and in the Southern part of the peninsula. Sizable red areas cover also most of Sicily; notably, the only High-High hot spots in the North of Italy are in Alto Adige. The rest of Northern Italy is characterized by a diffuse presence of blue Low-Low clusters of significantly low values of IVSM. To enhance interpretation in terms of seismic risk, contour-lines



Figure (3) LISA maps for IVSM: (a) is the univariate LISA map for IVSM, (b) the High-High, Low-Low hot-spots of the univariate LISA map stratified by ag[max] class

of ag[max] have been superimposed to the LISA map in Figure 3a, identifying through dashed lines the regions of high, medium, moderate and low seismic hazard (see Section 2). Figure 3b shows the stratification of the High-High and Low-Low hot spots displayed in Figure 3a, according to two macro-classes of ag[max], namely severe hazard (high/medium) and mild hazard (moderate/low). Here, the spatial clusters colored in red identify municipalities where significantly high values of IVSM are associated to a severe seismic hazard, their compounded action thus increasing the overall seismic risk. These are most of the municipalities of the South of Italy already detected in the LISA map of IVSM because of their high vulnerability. Exceptions are the yellow-colored municipalities of Figure 3b, where seismic hazard is mild. Note also the green hot spots in the North, notably in Friuli and Veneto, where a severe seismic hazard is associated with significantly low values of IVSM. For these municipalities, the low value of IVSM partially compensates the seismic hazard and contributes to the overall decrease of seismic risk.

4 Population growth and ageing, and social vulnerability

Almost a quarter of the Italian population lives in an Inner Area [31]. These are rural areas characterized by their distance from the main centers of services (education, health and mobility) and including almost half of the Italian municipalities. In the last decades, Italian Inner Areas have experienced a pronounced demographic decline and population ageing. These phenomena provide further indications of a fragile community which we believe should be taken into account when evaluating seismic risk and precision policies for reducing it. IVSM does not include such factors, which therefore deserve a separate analysis.

The MRCI captures the demographic dynamics of each municipality by re-



Figure (4) Maps of Italy where each municipality has been colored according to its VAR_PERC and ETA_Q3 , respectively

porting the percentage variation of the number of its residents in 2018 and 2011, that is the proportion between the difference of number of residents in the two years and the number of residents in 2011, multiplied by 100. In the MRCI this index is called VAR_PERC. The age distribution of the residents of a municipality is instead described through its quartiles, as of 2018. Figure 4 shows two maps of Italy: on the left, each municipality is colored according to VAR_PERC whereas on the right the color of each municipality corresponds to the value of the third quartile of the age distribution of its residents, called $ETA_{-}Q3$. The values of the global Moran's I statistic for VAR_PERC and ETA_Q3 are equal to 0.401 and 0.623, respectively. By inspecting the two maps, it is immediately obvious that the two indexes are strongly correlated, the demographic decline of the population being correlated with its ageing. A different perspective on this first qualitative observation, is given by Figure 5 where, for each municipality, VAR_PERC and ETA_Q3 are plotted against the value of seismic hazard ag[max], and each municipality is colored according to the log_{10} of its current resident population size $(log_{10}(POP))$. One may notice that municipalities with a larger population have a higher growth rate and a younger population (i.e., a lower value of ETA_Q3). In general, municipalities with a small number of residents appear older and affected by a pronounced demographic decline. The charts also show that these fragile communities characterize the landscape subject to high seismic hazard.

Aiming at the identification of significant spatial hot spots, we plot the LISA maps of VAR_PERC and ETA_Q3 in Figure 6. In Figure 6a, the High-High hot spots of VAR_PERC indicate a significantly positive growth rate for the population size. They are located in proximity of major urban attractors, in the North East of Italy with the notable addition of areas in Trentino and Alto Adige, in some coastal areas of the South of Italy and the main islands. Low-Low hot spots are instead located in the inner areas of the country. The picture is almost replicated in Figure 6b, with colors of opposite sign, where the LISA map for



Figure (5) Demographic decline and ageing of Italian municipalities projected on the seismic landscape: in map (a) each municipality is represented by its ag[max] and the value of VAR_PERC , in map (b) each municipality is represented by its ag[max] and the value of ETA_Q3 . The color of each municipality corresponds to the log_{10} of its resident population.

 ETA_Q3 is shown. Hot spots of significantly high values for ETA_Q3 indicate areas of ageing populations and are in good agreement with those identifying areas of population decline in Figure 6a. The Low-Low hot spots indicating areas with a younger resident population often correspond to areas characterized by a positive growth in Figure 6a.

To project this analysis on the seismic landscape, we plot in Figure 7 the LISA maps of Figure 6 stratified according to the two macro-classes of ag[max] identifying severe and mild seismic hazard. Areas where a severe seismic hazard (high or medium values of ag[max]) are associated with a negative growth rate of the population are of particular concern for seismic risk prevention and reduc-



Figure (6) Univariate LISA maps: in map (a) that for VAR_PERC , in map (b) that for ETA_Q3 .



Figure (7) The High-High, Low-Low hot-spots of univariate LISA maps stratified by ag[max] class: in map (a) that for VAR_PERC , in map (b) that for ETA_Q3 .

tion; these are the green hot spots in Figure 6a. The same concern applies to the red hot spots in Figure 6b, identifying areas where a severe seismic hazard is significantly associated to an ageing population. For many of these areas, particularly those belonging to the inner areas of the Appenine, there is a complete overlap with the green hot spots in Figure 6a, thus indicating communities where old age and a decreasing population add up to the their fragility in the face of a relevant seismic hazard.

5 The building stock age

Human communities live in buildings, and building vulnerability is the first and most important component of any assessment of seismic risk. In this vein, the main efforts of the Casa Italia project was to envision the quantitative basis to design efficient and effective precision policies incentivizing the reduction of vulnerability of the heterogenous building stocks of the Italian municipalities [28], thus promoting the safety of their communities against seismic risk. We argue that building stock vulnerability, as measured by its age distribution, should also be considered when evaluating the social and material vulnerability of a community. An old building stock – in Italy, often composed of historical buildings which cannot be demolished and reconstructed – requires large interventions for enhancing its quality against seismic shaking. The inability of a community to put in place such preventive actions, favoured by its demographic decline and ageing, adds to its overall fragility.

For each municipality, the MRCI summarizes the age of its building stock by reporting the relative frequencies of buildings constructed in each of the following nine disjoint time classes: before 1919; 1919-1945; 1946-1960; 1961-1970; 1971-1980; 1981-1990; 1991-2000; 2001-2005; after 2005. See, for instance, Figure 8 for



Figure (8) Building stock distribution for the municipality of Milan

the distribution of time-of-construction of the building stock of Milan. Time-ofconstruction is an important indicator of building vulnerability since anti-seismic regulations, enforcing higher standards for building quality against earthquake shaking, have been introduced in Italy between 1981 and 1984 and then again in 2003: see [28].

For the analysis of the variability of the time-of-construction distributions of the building stock of the Italian municipalities, we note that these are compositional data which belong to the simplex of R^9 . Indeed, the time-of-construction distribution for the buildings of the *i*-th municipality is a vector of p = 9 positive components $\underline{x}_i = (x_1, ..., x_p)'$ summing up to 1. The vector \underline{x}_i belongs to the simplex S^p , a subset of R^p :

$$S^{p} = \left\{ \underline{x} = (x_{1}, \dots, x_{p})' \in R^{p} : x_{j} > 0 \text{ for } j = 1, \dots, p, \ \sum_{j=1}^{p} x_{j} = 1 \right\}.$$

Aitchison (1982) [1] firstly proposed the use of a log-ratio approach to the analysis of compositional data, defining a set of principles that such analyses should fulfill (see [25, 24, 26]). These principles led to the definition of a specific geometry for S^p , named Aitchison geometry, which is built upon two main operations, perturbation and powering defined, for $\underline{x}, y \in S^p$, as

$$(\underline{x} \oplus \underline{y})_j = \frac{x_j y_j}{\sum_{k=1}^p x_k y_k}; \ (\alpha \odot \underline{x})_j = \frac{x_j^{\alpha}}{\sum_{k=1}^p x_k^{\alpha}},$$

and an inner product

$$\langle \underline{x}, \underline{y} \rangle = \frac{1}{2p} \sum_{j=1}^{p} \sum_{k=1}^{p} \ln \frac{x_j}{x_k} \ln \frac{y_j}{y_k},$$

implying a norm and a distance within the space. Note that the neutral element of perturbation is the uniform composition, i.e., $\underline{0}_{\oplus} = (1/p, ..., 1/p)'$.

The simplex S^p endowed with the Aitchison's geometry is a finite-dimensional Hilbert space, which is isometrically isomorphic to the linear space $M \subset R^p$, of dimension p-1, consisting of those vectors of R^p whose components sum up to 0. The isomorphism is, for instance, provided by the *centered log-ratio* transformation (clr) defined, for $\underline{x} \in S^p$, as

$$clr(\underline{x}) = \left[\ln\left(\frac{x_1}{(\prod_{j=1}^p x_j)^{1/p}}\right), \dots, \log\left(\frac{x_p}{(\prod_{j=1}^p x_j)^{1/p}}\right) \right]'.$$
 (3)

Since building stock data are constrained objects, the overall effect of the seismic hazard factor, whose levels are the four classes listed in Section 2, on the distribution of building stock compositions is here assessed through a *compositional* one-way ANOVA. For the time-of-construction composition \underline{x}_{is} of the building stock of the *i*-th municipality in the *s*-th class of seismic hazard, we thus consider the model

$$\underline{x}_{is} = \underline{\mu} \oplus \underline{\tau}_s \oplus \underline{\epsilon}_{is},\tag{4}$$

with $\underline{\mu}$ the overall mean, $\underline{\tau}_s$ the effect of the *s*-th level of the seismic hazard factor, and $\underline{\epsilon}_{is}$ zero-mean i.i.d. errors. To test the significance of the $\underline{\tau}_s$, we set the hypothesis

$$H_0: \underline{\tau}_1 = \dots = \underline{\tau}_4 = \underline{0}_{\oplus} \quad \text{against} \quad H_1: \text{ at least one } \underline{\tau}_s \neq \underline{0}_{\oplus}, \tag{5}$$

and we perform a permutational ANOVA test, that allows coping with the non-Gaussianity of the errors [4, 27]. From the computational standpoint, the test is run by first transforming the data thorough the clr function defined in (3), which yields a set of (constrained) data $\{clr(\underline{x}_{is}), i = 1, ..., n_s, s = 1, ..., 4\}$ in the linear space $M \subset \mathbb{R}^p$, where n_s stands for the number of municipalities belonging to the s-th level class of seismic hazard. Due to the isometric nature of the clr transformation, the following model in \mathbb{R}^p for the $clr(\underline{x}_{is})$'s is consistent with (4)

$$clr(\underline{x}_{is}) = clr(\mu) + clr(\underline{\tau}_s) + clr(\underline{\epsilon}_{is}).$$
(6)

On the transformed model, the hypotheses (5) read

$$H_0: clr(\underline{\tau}_1) = \dots = clr(\underline{\tau}_4) = \underline{0}$$
 against $H_1:$ at least one $clr(\underline{\tau}_s) \neq \underline{0}.$ (7)

The test is run using the pseudo-F statistic

$$F = \frac{(SS_T - SS_W)/(4-1)}{SS_W/(n-4)},$$

where SS_T is the total sum-of-squares and SS_W is the within groups sum-of-

squares:

$$SS_T = \frac{1}{n} \sum_{i=1}^{n-1} \sum_{j=i+1}^n d_{ij}^2,$$

$$SS_W = \frac{1}{n} \sum_{i=1}^{n-1} \sum_{j=i+1}^n d_{ij}^2 \delta_{ij}.$$

Here d_{ij} indicates the Euclidean distance between clr-transformed observations i, j, while $\delta_{ij} = 1$ if observations i and j belong to the same group and 0 otherwise [3][4].

The distribution of F under H_0 is obtained by permuting the transformed data, as advocated in [27]. Under H_0 , the pseudo-F statistic exceeds its observed value $F_0 = 54.35$ in the sample with an estimated frequency equal to 0.001. The routines that implement the test performed with the R package vegan [22] are freely available in the github account indicated in the Introduction; they have been run by setting the number of permutations equal to 1000. The result supports the claim that the effect of the seismic hazard factor on the distribution of the time-of-construction compositions is significant.

We further investigate this issue, by exploring the spatial distribution of the time-of-construction compositions of the building stock through effective compositional summaries. Indeed, we reduce the dimensionality of the of the time-of-construction compositions by eliciting the main direction of their variability via a Compositional Principal Component Analysis [2] performed with the R package compositions [33].

Figure 9 shows the first principal component scores - a variable called PC1 in the following - and projections, this principal component explaining the 45% of the variability of the time-of-construction compositions. The guide chart in Figure 9b reports in black the average building stock composition for Italian municipalities, computed according to the Aitchison geometry in S^9 . This barycentric distribution has score equal to 0 in the direction of the first principal component. The colored distributions appearing in the same chart correspond to distributions lying on the first principal component direction and identified by a score ranging from $-5\sqrt{\lambda_1}$ to $+5\sqrt{\lambda_1}$, $\sqrt{\lambda_1} = 1.67$ being the standard deviation of the data scores along the first principal component. Low score values (cold colors) indicate time-of-construction distributions concentrated on more recent years (i.e. a young building stock) whereas high score values (hot colors) correspond to time-of-construction distributions more concentrated in the long past (i.e. an old building stock). This chart guides the reading of the Italian map in Figure 9a, where each municipality is colored according to PC1. Colors indicate the correspondence between scores, as represented on the Italian map in Figure 9a. and time-of-construction distributions plotted in the guide chart in Figure 9b. Municipalities with a cold color have a younger building stock, those colored with hot colors an older one.

To emphasize the impact of anti-seismic regulations, we aggregate the time classes defining the time-of-construction distributions in three macro time in-



Figure (9) Building stock age: in map (a) each municipality has been colored according to the PC1 score of the time-of-construction distribution of its building stock, map (b) reports the guide chart associating scores with time-ofconstruction distributions.

tervals: before 1919 (very old buildings), between 1919 and 1980 (more recent buildings, constructed before the anti-seismic regulations), after 1980 (buildings constructed while or after anti-seismic regulations were introduced in Italy). These time-of-construction ternary distributions, one for each Italian municipality, can be represented as points belonging to the simplex S^3 . The data cloud appears in Figure 10a. Reported on the simplex are also the directions of their two principal components, which define a basis for S^3 and which intersect at the barycentric distribution, corresponding to the average ternary distribution of time-of-construction for Italian municipalities. The first principal component (PC1) explains 86% of the data variability; by moving along the PC1 direction, passing from positive (hot) scores to negative (cold) scores, one visits time-ofconstruction ternary distributions first concentrated on the "before 1919" class and then more and more concentrated on the "after 1980" class, as is also shown in the guide chart in Figure 10b. Figure 10c represents each Italian municipality colored according to the score of its time-of-construction ternary distribution on the PC1 represented in Figure 10a and 10b. One could consider this map of Italy as a coarse summary of the map in Figure 9. Notice, in particular, the areas of the country where the building stocks are of more recent time of construction (colored in blue); among the obvious metropolitan areas, the Irpinia region and some areas of Friuli stand out, both regions having been vastly reconstructed after the tragic earthquakes of 1976 and of 1980, which prompted the Italian Parliament to pass anti-seismic regulations.

Coming back to the analysis of the complete time-of-construction distributions of the building stocks, data points of S^9 , the global Moran's I statistic measuring the spatial association of their PC1 scores is equal to 0.506. To single out the country's hot spots with respect to the age of their building stock, we represent, in Figure 11a, a univariate LISA map of the PC1 scores pictured in Figure 9a. The map clearly points out the Low-Low clusters of more recent building stock: the large metropolitan attractors of demographic expansion around Milan



Figure (10) Building stock age: each point in the simplex shown in map (a) represents the ternary distribution of the time-of-construction of the building stock of an Italian municipality. The basis formed by the two principal components is shown; PC1 and PC2 cross at the average ternary distribution. The colors of the scores identifying points on the PC1 axis correspond to the colors of the distributions appearing in the guide chart (b) on the right. In map (c) each municipality is colored according to the PC1 score of the ternary distribution of the time-of-construction of its building stock.



Figure (11) Building stock age. (a) Univariate LISA map of the PC1 scores of the complete time-of-construction distributions; dashed lines represent the boundaries among classes of seismic hazard. (b) the High-High, Low-Low hot-spots of the univariate LISA map of the PC1 scores of the complete time-of-construction distributions stratified by ag[max] class.

and Rome, the North East, the coasts of Sardinia witnessing the development of its tourism industry, the already mentioned reconstructed Irpinia and Friuli regions, and notable spots in Sicily, Puglia and Calabria. The High-High hot spots identifying areas characterized by an ageing building stock run along the inner areas of the Appenines and also single out large portions of Piedmont, with the exception of the territory surrounding Turin, of Liguria and of Tuscany. Figure 11b segments these hot spots according to the two macro-classes of seismic hazard (severe/mild). Whereas the green Low-Severe clusters indicate areas of the country where seismic hazard is severe but seismic risk is attenuated by a more recent building stock, concern is generated by the red High-Severe areas where a medium or high seismic hazard is associated with an ageing building stock. Once again these red areas belong to the inner regions of the country characterized by small communities, already suffering from a demographic decline and ageing of their residents. To elaborate on this point, consider Figure 12. Each municipality appears as a point colored according to the \log_{10} of its resident population; on the abscissa the seismic hazard associated to the municipality, on the ordinate axis the PC1 score. One notices immediately the overwhelming presence of communities with less than 10000 residents among those with extremely low values for the PC1 score and therefore an ageing building stock. This evidence is even more compelling for those municipalities with a high seismic hazard (aq[max] > 0.25q).

6 An aggregated analysis

Given the bounded resources constraint, policy makers need to prioritize their interventions against social and material vulnerability if they want to implement efficient precision policies. Indeed, "the necessity to develop methods and indi-



Figure (12) Building stock age: PC1 versus ag[max].

cators (to assess social vulnerability)... which can be used in policy and decisionmaking processes" has been stressed also in [7]. With this goal in mind, we try in this section to aggregate the results of the previous analyses with the aim of eliciting a conceivable global picture of social and material vulnerability in the face of seismic hazard for the Italian municipalities.

One obvious line of attack would be to single out those municipalities simultaneously troubled by a high IVSM value, demographic decline and an old building stock. To this effect, we set the threshold $t_{IVSM} = 100.29$ equal to the third quartile of the IVSM distribution over the Italian municipalities, the threshold $t_g = -4.64\%$ equal to the first quartile of VAR_PERC and finally the threshold $t_b = 1.18$ equal to the third quartile of the PC1 score of the complete time-of-construction distributions of the building stock. Given the collinearity between VAR_PERC and ETA_Q3 we decided to use only one of the two variables in the criterion for selecting municipalities; we settled on the former because it allows a better outlook on the future fragility of a community as it captures the demographic dynamics of its resident population. We then highlight in Figure 13 those municipalities with:

$$IVSM \ge t_{IVSM}$$
 and $VAR_PERC \le t_q$ and $PC1 \ge t_b$. (8)

Out of 7953 municipalities, 247 pass the selection criterion (8). This supports the assumption of a very mild dependence for the three variables IVSM, VAR_PERC and PC1 since, in case of independence, we expect only 125 ± 23 municipalities to pass 8. The selected municipalities, highlighted in Figure 13, are colored according to their membership to one of the four classes of seismic hazard as defined in Section 2, and identified by the contour lines on the plot. Their distribution in the four seismic classes is reported in Table 1; one may notice that for almost 70% of them, the seismic hazard is medium or high.

A second line of attack aims at a global ranking of the Italian municipalities in line with the three indexes we have so far considered for capturing social and material vulnerability; for this, we will use the Copeland method illustrated in [19]. First, we separately rank the municipalities consistently with IVSM,



ag[max] class	Proportion
(0,0.05]	0.07
(0.05, 0.15]	0.26
(0.15, 0.25]	0.46
(0.25, 0.35]	0.21

Figure (13) Map of Italy where each selected municipality has been colored according to ag[max] class.

Table (1) Proportion of municipalities being selected for each class of ag[max].

VAR_PERC and the PC1 scores of their complete time-of-construction distributions of building stock. For ranking municipalities according to IVSM and PC1, we proceed in ascending order, attributing rank 1 to the municipality with the smallest index, that is the best in terms of IVSM or PC1 score, respectively. Ranking of municipalities according to VAR_PERC proceeds instead in descending order, rank 1 being attributed to the municipality having highest VAR_PERC , that is the best in terms of demographic growth. Ties are sorted by population size, a smaller population size inducing a larger rank number. In other words, in each of the three rankings, larger rank numbers are indicative of a higher vulnerability, as captured by the indexes analyzed in the previous sections of this paper. To obtain a final global ranking, we then consider all pairwise competitions between municipalities. When municipality *i* competes against municipality *k*, let r_{il} and r_{kl} be their respective rank numbers in the rankings l = 1, 2, 3, described above and set the result of the competition to be

$$s_{i,k} = \begin{cases} 1, & \text{if } \#\{l \in \{1,2,3\} : r_{il} > r_{kl}\} \ge 2; \\ -1, & \text{if } \#\{l \in \{1,2,3\} : r_{il} > r_{kl}\} \le 1. \end{cases}$$
(9)

Finally, for i = 1, ..., n, we compute the Copeland score of the municipality i as the sum over the results of all pairwise competitions,

$$C_i = \sum_{k \neq i} s_{i,k}.$$

Figure 14 shows the map of Italy where each municipality has been colored according to its Copeland score, hot colors for the units with a high score, i.e. worse off in our global ranking of social and material vulnerability, cold colors for those municipality with a low Copeland score, better off in terms of social and material vulnerability. The contours defining the four classes of seismic hazard are also reported. We can see that the ranking provided by the Copeland score highlights vulnerable areas in Piedmont, in Friuli and in the inner regions of Apennines and of the main islands, consistently with our previous analyses.



Figure (14) Map of Italy where each municipality has been colored according to the Copeland score.

One may also notice that the areas characterized by high Copeland scores are frequently concurrent with the areas of severe seismic hazard. To elaborate on this consider Figure 15 which depicts as boxplots the conditional distributions of the Copeland score, given the values of ag[max] defining the four seismic classes listed in Section 2. There is a clear stochastic order among the four distributions, those associated to larger values of ag[max] dominating those corresponding to less hazardous areas. Therefore, for municipalities belonging to the medium or high seismic hazard classes, social and material vulnerability is acting as an amplifier of seismic hazard, contributing to the increase of risk instead of dimming it.

Ultimately, ranking through the Copeland's score allows to prioritize the public intervention on Italian municipalities, with the goal of reducing their vulnerability to seismic hazard. Each community is however different, and the multidimensional analysis carried out in the previous sections allows to discriminate among the components which differentially contribute to the social and material vulnerability of Italian municipalities, profiling each municipality in terms of its dominant fragilities when exposed to a seismic event, and allowing decision makers to plan tailored precision policies to fight them. This is in contrast to the actual policies designed to reduce seismic risk, which focus only on the hazard factor and cluster the municipalities in terms of the four hazard classes listed in Section 2, promoting and incentivizing prevention against the risk by means of equal measures shared by all municipalities belonging to the same cluster.



Figure (15) Conditional distributions of Copeland score, given ag[max].



Figure (16) Temporal population dynamics: in (a) each municipality is represented by the log growth curve, colored according to the ag[max]. In (b) curves are year-wise medians of the log growth rates for the four ag[max] classes. Note that different scales are used for the y-axes in plots (a) and (b), to enhance visibility of the curves.

7 Discussion and further supporting analyses

In the previous section, we claimed that VAR_PERC allowed a better outlook on the future fragility of a community because it captures the demographic dynamics of its resident population. We thus used this variable, instead of the correlated ETA_Q3 , when building a global ranking of the Italian municipalities in terms of social and material vulnerability. Although MRCI provides, through VAR_PERC , the variation of the number of residents between 2011 and 2018, the resident population of every municipality is constantly monitored by ISTAT. In fact, based on the data made public by ISTAT, for every Italian municipality we know the annual demographic growth between 1992 and 2012.

Figure 16, on the left, shows for each Italian municipality the log of the ratio between its population size in a given year and its population size in 1992, taken as reference year, that is the log of its demographic proportional growth



Figure (17) Proportional growth curves: in (a) each municipality has been colored according to the the score of its log proportional growth curve on the first Functional Principal Component. The score color identifies the corresponding log proportional growth curve on the guide chart (b).

with respect to 1992. Each curve is colored according to the aa[max] associated to the municipality. One might notice that for many municipalities troubled by a medium or high seismic hazard the population is not increasing, when it is not steadily declining. Indeed this is confirmed by the graph on the right where, for the four seismic hazard classes, the medians of the log proportional growths are represented for every year. After smoothing the log of the demographic proportional growth curves by means of 11 cubic B-splines, we performed a Functional Principal Component Analysis [29]. The first principal component captures 95.4% of the data variability, thus supporting their projection on a 1dimensional linear subspace, where each curve is encapsulated in a real number, its score on the first principal component. Figure 17 shows the map of Italy, where each municipality has been colored according to these scores; on the right the guide chart for interpreting the values of the scores, cold colors being associated to declining log proportional growth curves, hot colors otherwise. The black curve is the average log proportional growth curve for the entire country. These scores are correlated ($\rho = 0.94$) to the variation index VAR_PERC reported in the MRCI and analyzed in the previous sections, thus supporting the claim that VAR_PERC is tracking a long term trend of the local demographic dynamics.

A second point worth of discussion is the spatial variability of the index IVSM, analyzed in Section 3. It was already noted that IVSM shows a marked trend moving from the North to the South of the peninsula. Although less obvious, the careful reader of Figure 2 will also notice that the variability of IVSM between municipalities sharing a similar latitude is also changing when moving form North to South. To better support this claim, we looked at the IVSM data at a different spatial scale, considering provinces instead of municipalities. In fact, for each Italian province we may compute the distribution density of the value of IVSM observed for its municipalities. For better visualization and treatment, these distributions are then smoothed via kernel smoothing (Gaussian kernel, bandwidth = 0.527); they are depicted in Figure 18.



Figure (18) IVSM distributions for the Italian provinces. In (b) the six largest Italian provinces in terms of resident population, year 2018

A shift from dark purple to yellow corresponds to a shift from North to South, the colors being assigned on a regional basis. One may notice a strong spatial trend for both the location of the densities and their scale, when moving from North to South. This implies a large variability between provinces in terms of IVSM, provinces in the South of Italy and Sicily being associated to larger values of mean IVSM, but also an increasing heterogeneity within the provinces, the provinces in the South being characterized by a larger variability of the IVSMof their municipalities. To make this trend even more manifest, we ultimately explore the classification of provinces based on the distribution of IVSM among their municipalities. For any pair of provinces (P, Q), we compute the Wasserstein distance between the cumulative distributions F_P and F_Q of the IVSM for their municipalities:

$$d_W(P,Q) = \sqrt{\int_0^1 [F_P^{-1}(t) - F_Q^{-1}(t)]^2 dt}.$$

We then run the Agglomerative Hierarchical Clustering Algorithm with Ward linkage to obtain the dendrogram plotted in Figure 19. Cutting the dendrogram to obtain four clusters, we get the clusters of provinces represented in Figure 20, on the left, which seems to be in strong connection with the representation of IVSM offered by Figure 2. On the right of Figure 20, the barycentric distributions of the three clusters are reported; they clearly support the claim of a North-South regional trend for the IVSM provincial distributions, both in terms of location and of scale. The claim is also quantitatively supported by Table 2 where mean, standard deviations, and quartiles of these barycentric distributions are reported.

8 Conclusion

Social vulnerability is an abstract construct having multiple referents, none of which is fully comprehensive. By analyzing the data stored in the MRCI, we tried



Figure (19) IVSM: the dendrogram clustering provinces



Figure (20) $\ IVSM:$ provinces clustering using Wasserstein distance. In (b) barycenters of the four clusters

Cluster	Mean	\mathbf{sd}	$\mathbf{Q1}$	$\mathbf{Q2}$	Q3
1	97.09	1.74	96.13	96.93	97.80
2	98.80	1.44	97.92	98.72	99.54
3	100.29	1.58	99.29	100.20	101.13
4	102.43	2.67	100.68	102.08	103.76

Table (2) Summary indices of IVSM within the clusters of provinces.

to capture a concept of social and material vulnerability which is functional to the design of precision policies for the prevention and reduction of the seismic risk of Italian municipalities. Encompassing *IVSM*, we also considered as referents of social and material vulnerability the demographic dynamics of the communities and the age of the building stock where the community resides, grounding our argument on the belief that an aging and demographically declining community, living in buildings requiring significant improvements to be brought to safety, is more fragile and vulnerable when confronted with a seismic catastrophic event. Fusing measurements of different factors associated to the latent social and material vulnerability, we formulated a tentative ranking of Italian municipalities apt to prioritize the public intervention for prevention and reduction of their seismic risk by means of precision policies rooted in their different fragility profiles, elicited by our multidimensional analysis.

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